

Determining the Chemical Composition of Solid Waste





Problem Statement

Determine the chemical composition of the organic fraction of the waste described in Table 1, with and without sulfur and with and without water.



Table 1. Composition of Solid Waste

| Component | Wet Weight, lb | Percent MC |
|------------------|-----------------------|-------------------|
| Food Wastes | 9 | 70 |
| Paper | 34 | 6 |
| Cardboard | 6 | 5 |
| Plastics | 7 | 1 |
| Textiles | 2 | 10 |
| Rubber | 0.5 | 0 |
| Leather | 0.5 | 20 |
| Yard wastes | 18.5 | 65 |
| Wood | 2 | 20 |
| Inorganic | 20.5 | 3 |



Step 1: Calculate the Weight of Each Element

- Using data in Table 2, calculate the weight of C, H, O, N, S, and ash in each component
- Table 2 is based on dry waste only, first the dry weight of each component must be calculated
- Results are presented in Table 3

Table 2. Chemical Composition of Waste Components

TABLE 2
Typical data on the ultimate analysis of the combustile components in residential MSW^a

| Component | Percent by weight (dry basis) | | | | | Ash |
|---------------------|-------------------------------|----------|--------|----------|--------|------|
| | Carbon | Hydrogen | Oxygen | Nitrogen | Sulfur | |
| Organic | | | | | | |
| Food wastes | 48.0 | 6.4 | 37.6 | 2.6 | 0.4 | 5.0 |
| Paper | 43.5 | 6.0 | 44.0 | 0.3 | 0.2 | 6.0 |
| Cardboard | 44.0 | 5.9 | 44.6 | 0.3 | 0.2 | 5.0 |
| Plastics | 60.0 | 7.2 | 22.8 | — | — | 10.0 |
| Textiles | 55.0 | 6.6 | 31.2 | 4.6 | 0.15 | 2.5 |
| Rubber | 78.0 | 10.0 | — | 2.0 | — | 10.0 |
| Leather | 60.0 | 8.0 | 11.6 | 10.0 | 0.4 | 10.0 |
| Yard wastes | 47.8 | 6.0 | 38.0 | 3.4 | 0.3 | 4.5 |
| Wood | 49.5 | 6.0 | 42.7 | 0.2 | 0.1 | 1.5 |
| Inorganic | | | | | | |
| Glass ^b | 0.5 | 0.1 | 0.4 | <0.1 | — | 98.9 |
| Metals ^b | 4.5 | 0.6 | 4.3 | <0.1 | — | 90.5 |
| Dirt, ash, etc. | 26.3 | 3.0 | 2.0 | 0.5 | 0.2 | 68.0 |

^aAdapted in part from Ref. 6.

^bOrganic content is from coatings, labels, and other attached materials.



Step 1: Sample Calculation

➤ Food Waste

$$MC = 70\%$$

$$9 - 9(0.7) = 2.7 \text{ lb dry weight}$$

$$\text{Carbon: } 2.7 (0.48) = 1.3 \text{ lb}$$

$$\text{Hydrogen: } 2.7 (0.064) = 0.17 \text{ lb}$$

Table 3. General Composition of Solid Waste

| Component | Wet Weight | Dry Weight | Composition | | | | | Ash |
|--------------|-------------|-------------|--------------|-------------|--------------|-------------|-------------|-------------|
| | lb. | lb. | C | H | O | N | S | |
| Food Waste | 9.0 | 2.7 | 1.30 | 0.17 | 1.02 | 0.07 | 0.01 | 0.14 |
| Paper | 34.0 | 32.0 | 13.90 | 1.92 | 14.06 | 0.10 | 0.06 | 1.92 |
| Cardboard | 6.0 | 5.7 | 2.51 | 0.34 | 2.54 | 0.02 | 0.01 | 0.29 |
| Plastic | 7.0 | 6.9 | 4.16 | 0.50 | 1.58 | 0.00 | 0.00 | 0.69 |
| Textiles | 2.0 | 1.8 | 0.99 | 0.12 | 0.56 | 0.08 | 0.00 | 0.05 |
| Rubber | 0.5 | 0.5 | 0.39 | 0.05 | 0.00 | 0.01 | 0.00 | 0.05 |
| Leather | 0.5 | 0.4 | 0.24 | 0.03 | 0.05 | 0.04 | 0.00 | 0.04 |
| Yard Wastes | 18.5 | 6.5 | 3.10 | 0.39 | 2.46 | 0.22 | 0.02 | 0.29 |
| Wood | 2.0 | 1.6 | 0.79 | 0.10 | 0.68 | 0.00 | 0.00 | 0.02 |
| TOTAL | 79.5 | 58.1 | 27.37 | 3.61 | 22.95 | 0.54 | 0.11 | 3.48 |



Step 2. Calculate the weight of H and O in water

- From Table 2 we see that **dry waste** has a weight of 58.1 pounds, and that **discarded-waste** has a weight of 79.5 pounds.
- We then subtract the weight of the dry waste from the weight of the saturated waste to give us the weight of the water in the waste.

$$79.5 \text{ lbs} - 58.1 \text{ lbs} = 21.4 \text{ lbs H}_2\text{O}$$





Step 2: Continued

We now want to determine how much hydrogen and oxygen in pounds there are in the waste sample. We do this by using the equation:

$$\left[\frac{\textit{Total _ Moisture _ in _ lb}}{\textit{molecular _ wt _ of _ water}} \right] x \textit{molecularwt _ of _ H}$$



Step 2: Continued

$$\left[\frac{21.4lb}{18lb} \right] * 2 = 2.38lb \text{ } _H$$

Similarly for Oxygen:

$$\left[\frac{21.4lb}{18lb} \right] * 16 = 19.02lb \text{ } _O$$



Step 2: Continued

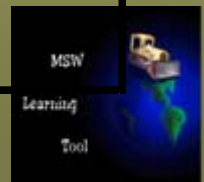
The amount of Hydrogen and Oxygen should be added to the H and O in the waste when we are calculating chemical composition with water. See Table 4.



Table 4. Percentage Distribution of the Elements with and without Water

| Element | lb, w/o Water* | lb, w/ Water |
|----------------|-----------------------|---------------------|
| Carbon | 27.37 | 27.37 |
| Hydrogen | 3.61 | 5.99 |
| Oxygen | 22.95 | 42.00 |
| Nitrogen | 0.54 | 0.54 |
| Sulfur | 0.11 | 0.11 |
| Ash | 3.48 | 3.48 |

*Row 11, Table 3





Step 4: Determine Molar Composition of the Elements, Neglecting Ash

- We do this by dividing each component by its respective molecular weight
- Results in Table 5

Table 5. Molar Composition

| Element | Atomic wt | Moles | Moles |
|----------|-----------|-----------|----------|
| | | W/O Water | W/ Water |
| Carbon | 12.01 | 2.279 | 2.279 |
| Hydrogen | 1.01 | 3.575 | 5.933 |
| Oxygen | 16.00 | 1.434 | 2.625 |
| Nitrogen | 14.01 | 0.038 | 0.038 |
| Sulfur | 32.07 | 0.003 | 0.003 |



Step 5. Determine Chemical Formula

- Determine the approximate chemical formula with and without sulfur and with and without water
- To determine the formula without sulfur, use the lowest represented element, nitrogen as the base; divide each value by the number of moles of nitrogen.
- Similarly, when determining the formula with sulfur use sulfur as a base and divide each by the number of moles of sulfur.
- See Table 6



Table 6. Normalized Mole Ratios

| Element | Mole Ratio - (Nitrogen = 1) | | Mole Ratio - (Sulfur=1) | |
|----------------|------------------------------------|-----------------|--------------------------------|-----------------|
| | W/O Water | W/ Water | W/O Water | W/ Water |
| Carbon | 59.2 | 59.2 | 655.8 | 655.8 |
| Hydrogen | 92.9 | 154.1 | 1028.8 | 1707.4 |
| Oxygen | 37.3 | 68.2 | 412.8 | 755.5 |
| Nitrogen | 1.0 | 1.0 | 11.1 | 11.1 |
| Sulfur | 0.1 | 0.1 | 1.0 | 1.0 |



Summary of Results

- The chemical formulas without sulfur are:
 - Without water: $C_{59}H_{93}O_{37}N$
 - With water: $C_{59}H_{154}O_{68}N$
- The chemical formulas with sulfur are:
 - Without water: $C_{656}H_{1029}O_{413}N_{11}S$
 - With water: $C_{656}H_{1707}O_{756}N_{11}S$
- Note: all values in whole numbers



On Your Own Problem

- Calculate the chemical composition of a typical yard waste with and without water (based on N and S)
- Hint: Assume 100 lb of waste, 40 % Moisture Content



Return to Home Page

Last updated July 2004 by Dr. Reinhart

